# Characterizing the Power of Moving Target Defense via Cyber Epidemic Dynamics

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#### **Moving Target Defense (MTD)**

■ MTD is believed to be "game changer."

☐ There are a bag of MTD techniques.

□ A classification of three classes (next slide)

#### **Three Classes of MTD**

- □ Network-based MTD Techniques
  - **❖ IP address and TCP port randomization etc.**
- ☐ Host-based MTD Techniques
  - Instruction-level: ISR
  - Code-level: code randomization
  - Memory-level: ASLR
  - Application-level: N-version programming etc
- ☐ Instrument-based MTD Techniques
  - Dynamic honeypot

#### **How to Characterize Power of MTD?**

- ☐ There is no systematic quantitative understanding of the power of MTD techniques individually, let alone collectively.
- □ Consequence: Don't know how to deploy them collectively and effectively or even optimally.
  - How to even define/formalize them exactly?
- ☐ This paper: Using cyber epidemic dynamics as the "lens" (or "ruler") to characterize power of MTD.
  - First analytic approach
  - First-step within this approach

#### What Is This Paper Basically About?

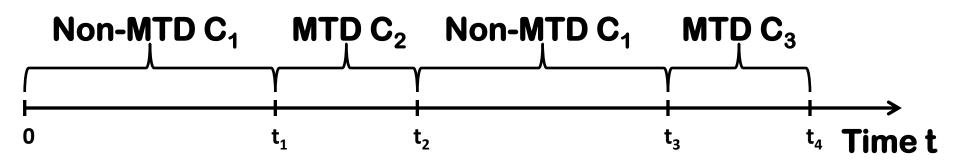
- □ Cyber system often stays in some insecure/undesired configuration/posture (will be precisely defined).
- MTD often induces transient secure configurations, which however do not last permanently.
- □ How can we exploit MTD-induced secure configurations to rescue/tolerate the insecure ones, by (e.g.) making the dynamics converge to the clean state?

#### What Is This Paper Basically About?

One sentence summary: Suppose we know MTD-induced

transient secure configurations, we can optimally

orchestrate MTD to achieve some desired long-term goal.



- □ C₁: insecure configuration (e.g., due to the introduction of new attacks)
- □ C<sub>2</sub>, C<sub>3</sub>, ...: MTD-induced transient secure configurations

#### **Optimal in What Sense?**

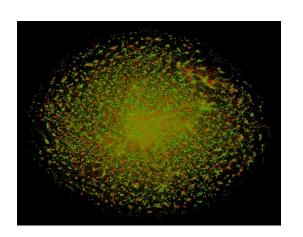
- ☐ Maximizing the time during which the cyber system can afford to stay in insecure configuration C₁, while still able to force the dynamics converge to the desired state.
  - Don't care about the cost imposed by launching MTD
- ☐ Minimizing the cost of deploying MTD, while allowing the cyber system to stay in insecure configuration for a given amount of time.
  - When cost matters

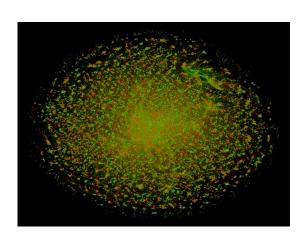
#### Roadmap

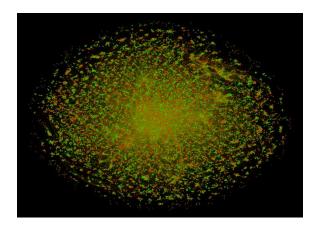
- □ Cyber epidemics model accommodating MTD
- $\square$  Analysis: The case of dynamic parameters  $\beta(t)$ ,  $\gamma(t)$
- □ Analysis: The case of dynamic structures G(t)
- □ Related work
- Conclusion and future research directions

A specific kind of Cybersecurity Dynamics (see poster) Complex Network based abstraction:

- □ Nodes abstract entities (e.g., computer)
  - \* Node state: green -- secure; red -- compromised
- □ Edges abstract the attack-defense interaction structure (system description/representation)



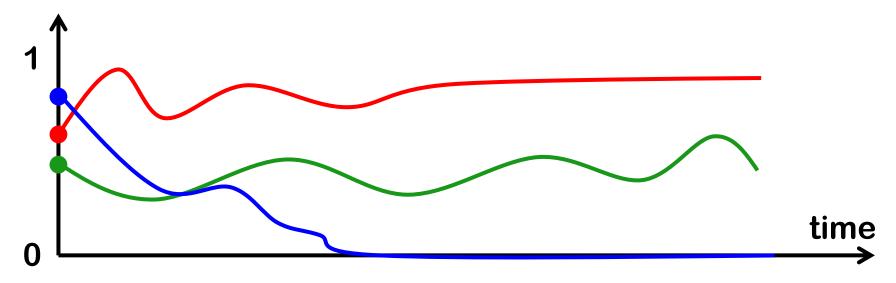




Three kinds of outcomes of evolution of global security state

Example Question: what are the governing/scaling laws?

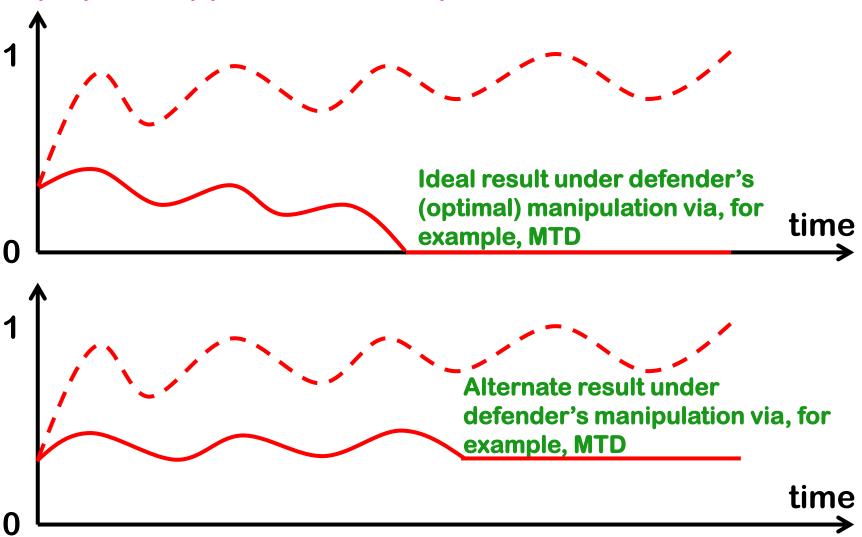
(Expected) portion of compromised nodes w.r.t. time



- ☐ This is perhaps the most natural *cybersecurity metric*.
- □ With information about the probability that the nodes are compromised at time t, we can make better decisions.

E.g., can a mission be disrupted at time t (< mission lifetime) with probability at most p?

(Expected) portion of compromised nodes w.r.t. time



Equilibria can be "dynamic" due to the introduction of zero-day attacks.

#### **Cyber Epidemics Model: Basics**

- □ Using attack-defense structure to capture the (attacker, victim) relation: G=(V, E)
- □ Using parameters to capture "atomic" attack and defense capabilities:
  - $ightharpoonup \gamma$ : the probability an infected node  $u \in V$  successfully attacks a secure node  $v \in V$  over  $(u,v) \in E$  at time t
  - β: the probability an infected node v becomes secure
     at time t

#### **Cyber Epidemics Model: Basics**

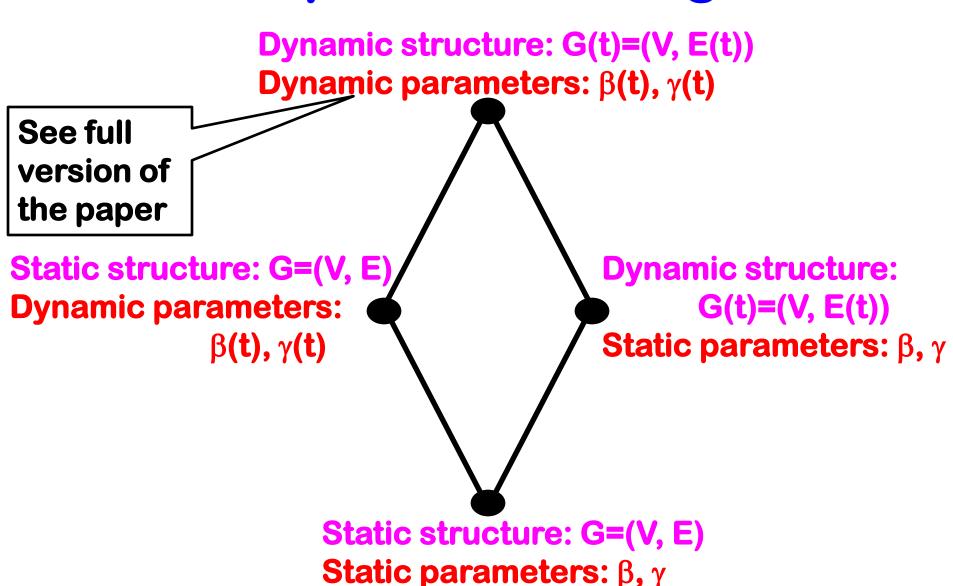
- ☐ Using attack-defense structure to capture the (attacker, victim) relation: G(t)=(V(t), E(t))
- Using parameters to capture "atomic" attacker and defense capabilities:  $\beta(t)$ ,  $\gamma(t)$
- □ Using epidemic threshold to describe the phase transition: sufficient condition under which the epidemic dynamics converges to equilibrium state the clean state (i.e., spreading dies out) in this paper.

#### **Cyber Epidemics Model with MTD**

Idea: MTD can induce dynamic attack-defense structures G(t)=(V(t), E(t)) and/or dynamic parameters  $\gamma(t)$  and  $\beta(t)$ 

- □ Network-based MTD Techniques can induce dynamic attack-defense structures (e.g., dynamic IP addresses)
- ☐ Host-based MTD Techniques can induce dynamic parameters (e.g., harder to penetrate into computers)
- ☐ Instrument-based MTD Techniques can induce dynamic attack-defense structures (e.g., dynamic IP addresses) and dynamic parameters (e.g., detecting new attacks)

#### **Problem Space: Assuming Fixed V**



**Definition: Configuration = (G(t), \beta(t), \gamma(t))** 

#### **A General Model**

- □ Dynamic structure: G(t)=(V, E(t)), adjacency matrix A(t)=[A<sub>vu</sub>(t)]
- $\Box$  Dynamic parameters:  $\beta(t)$ ,  $\gamma(t)$
- $\Box$  i<sub>v</sub>(t): probability node v is infected at time t (i.e., state)
- □ Assuming attacks are launched independently
  - See "a new approach to modeling and analyzing security ..." for tackling adaptiveness/dependence
- ☐ We have, *for each v*

$$\frac{di_{\nu}(t)}{dt} = \xi_{\nu}(t)(1 - i_{\nu}(t)) - \beta(t)i_{\nu}(t) 
= \left(1 - \prod_{u \in V} (1 - A_{\nu u}(t)i_{u}(t)\gamma(t))\right)(1 - i_{\nu}(t)) - i_{\nu}(t)\beta(t).$$

#### **Threshold in the Simplest Case**

Suppose both attack-defense structure time-invariant t: G = (V, E) with adjace

**Spreading dies** out (clean state)

The dynamics converges to equilibrium  $I^* = (0, ..., 0)$  if

$$I^* = (0, \dots, 0)$$
 if

$$\mu \stackrel{\text{def}}{=} \beta - \gamma \lambda_1(A) > 0, \tag{1}$$

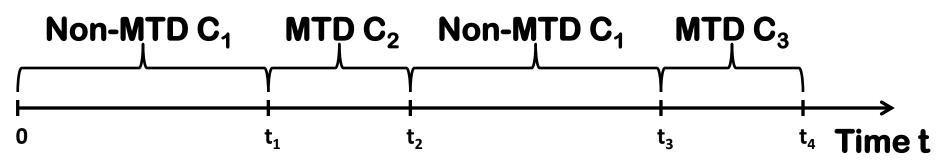
where  $\lambda_1(A)$  is the larges The threshold adjacent matrix A.

(sufficient condition)

le of the

If  $\mu < 0$ , the dynamics does not converge to  $I^* = (0, ..., 0)$  at least for some initial values.

#### Idea of Tolerating Insecure Config.



- Definition: Insecure configuration  $C_1=(G_1, \beta, \gamma)$ : because it violates convergence condition (1).
- □ Suppose the system has to stay in configuration C₁
  - Justification: introduction of new attacks etc.
- The defender can exploit MTD to force the system into some transient secure configuration C2, C3, ...
- How to orchestrate MTD to make the dynamics converge to the desired equilibrium state?

#### **Def: MTD-Power w/o Considering Cost**

#### **Definition**

 $((\mu_1, \mu_2, \dots, \mu_J, \pi_1^*)$ -powerful MTD, without considering cost) Denote by  $\mu_k = \beta_k - \gamma_k \lambda_1(A_k)$  for  $k = 1, \dots, J$ , where  $A_k$  is the adjacency matrix of  $G_k$ .

- 1. Undesired Given
  2. MTD induction maximize  $(\gamma_i, \gamma_i)$  with  $\mu_1 < 0$ .
- $j \geq 2$ .

We say MTD is  $(\mu_1, \mu_2, \dots, \mu_J, \pi_1^*)$ -powerful f it can make the overall dynamics converge to  $I^* = (0, \dots, 0)$ , while allowing the system to stay in configuration  $C_1$  for the maximum  $\pi_1^*$ -portion of time in the equilibrium.

#### **Def: MTD-Power while Considering Cost**

#### **Definition**

- $((\mu_1, \mu_2, \cdots, \mu_J, \pi_1, \Upsilon)$ -powerful, while considering cost) Consider cost function  $h(\cdot) : \mathbb{R}^+ \to \mathbb{R}^+$  such that  $h(\mu_j)$  is the cost of launching MTD to induce configuration  $\mathcal{C}_j$  for  $j = 2, \ldots, J$ , where  $h'(\mu) \geq 0$  for  $\mu > 0$ .
  - 1. Undesired Given potion of tin Given information To minimize  $\mu_1 < 0, \ \pi_1$  is the
- 2. MTD induced configurations  $C_i = (G_i, \beta_i, \gamma_i), \mu_j > 0, j \geq 2$ . We say MTD is  $(\mu_1, \mu_2, \cdots, \mu_J, \pi_1, \Upsilon)$ -powerful if the overall dynamics converges to  $I^* = (0, \dots, 0)$  at the minimum cost  $\Upsilon(\pi_2^*, \cdots, \pi_J^*)$ , where  $\pi_j^*$   $(2 \leq j \leq J)$  is the portion of time the system stays in configuration  $C_i$  in the equilibrium.

#### Roadmap

- Cyber epidemics model accommodating MTD
- $\square$  Analysis: The case of dynamic parameters  $\beta(t)$ ,  $\gamma(t)$
- □ Analysis: The case of dynamic structures G(t)
- □ Related work
- Conclusion and future research directions

#### **A General Result**

#### **Theorem**

(Xu et al., ACM TAAS 2014) Consider configurations  $(G, \beta(t), \gamma(t))$ , where  $(\beta(t), \gamma(t))$  are driven by a homogeneous Markov process  $\eta_t$  with steady-state distribution  $[\pi_1, \dots, \pi_N]$  and support  $\{(\beta_1, \gamma_1), \dots, (\beta_N, \gamma_N)\}$ , meaning

$$\mathbb{E}(\beta_{\eta_t}) = \pi_1 \beta_1 + \cdots + \pi_N \beta_N \text{ and } \mathbb{E}(\gamma_{\eta_t}) = \pi_1 \gamma_1 + \cdots + \pi_N \gamma_N. \text{ If }$$

$$\frac{\pi_1\beta_1+\cdots+\pi_N\beta_N}{\pi_1\gamma_1+\cdots+\pi_N\gamma_N}>\lambda_1(A),$$

the dynamics will converge to  $I^* = (0, ..., 0)$ ; if

$$\frac{\pi_1\beta_1+\cdots+\pi_N\beta_N}{\pi_1\gamma_1+\cdots+\pi_N\gamma_N}<\lambda_1(A),$$

the dynamics will not converge to  $I^* = (0, ..., 0)$  at least for some initial value scenarios.

#### Max Tolerance of Insecure Configuration without Considering MTD Cost

#### Theorem

For configurations  $C_j = (G, \beta_j, \gamma_j)$  with  $1 \le j \le N$ , we have  $\mu_j = \beta_j - \gamma_j \lambda_1(A)$  where  $\mu_1 < 0 < \mu_2 < \cdots < \mu_N$ . The maximal potion of time the system can afford to stay in configuration  $C_1$  is

$$\pi_1^* = \frac{\mu_N - \delta}{\mu_N - \mu_1},$$

which is reached by laund The optimal portions of time given by

orchestration strategy

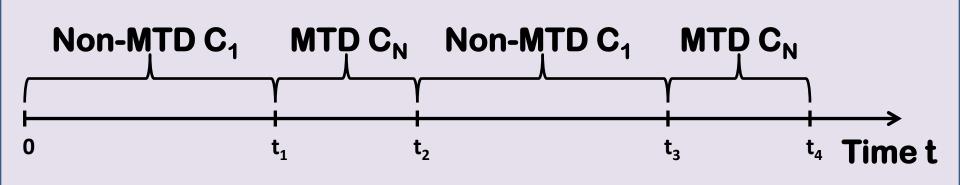
nly with

$$\pi_2^* = \dots = \pi_{N-1}^* = 0, \quad \pi_N^* = \frac{\delta - \mu_1}{\mu_N - \mu_1}.$$
 (2)

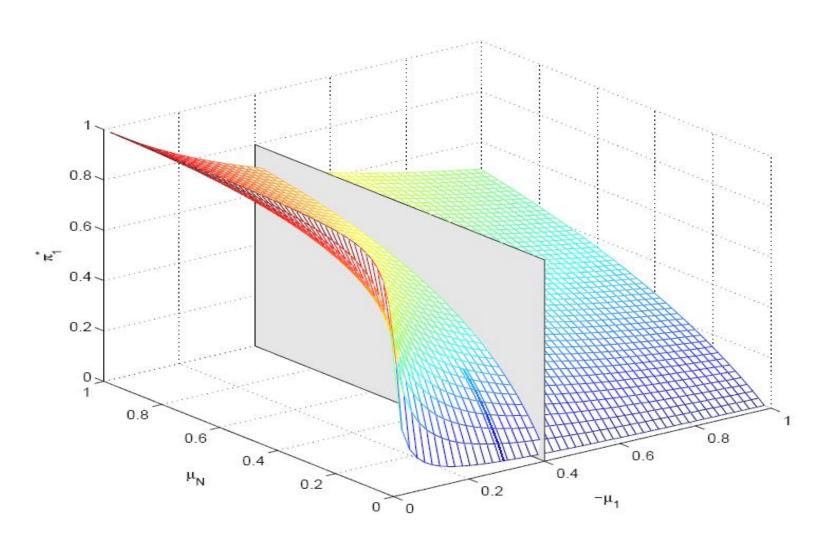
In other words, MTD is  $(\mu_1, \dots, \mu_N, \pi_1^*)$ -powerful.

## Algorithm for Orchestrating MTD to Achieve the Max Tolerance (without considering cost)

- 1. Compute  $\pi_1^*$  according to (2).
- while TRUE do
- 3. Wait for time  $T_1 \leftarrow \exp(a/\pi_1^*)$  {system in  $C_1$ }
- 4. Launch MTD to make system stay in  $C_N$  for time  $T_N \leftarrow \exp(a/(1-\pi_1^*))$
- 5. Stop launching MTD {system returns to  $C_1$ }



## Degree of Tolerance vs. Parameters: the case of not considering cost



Dependence of  $\pi_1^*$  on  $-\mu_1$  and  $\mu_N$ .

#### Minimizing Cost w.r.t. Given Degree

#### of Tolerance

Suppose  $\pi_1$  is the potion of time the system must stay in  $\mathcal{C}_1$ , it should satisfy  $0 < \pi_1 \le \frac{\mu_N - \delta}{\mu_N - \mu_1}$ .  $f(\cdot)$  is the cost function. The cost of launching MTD is

$$\Phi(\pi_2, \cdots, \pi_N) = \pi_1 f(\mu_1) + \sum_{j=2}^N \pi_j f(\mu_j).$$

Define

$$\mu_{k^*} = \min\left\{\mu_k | \mu_k > \frac{-\pi_1 \mu_1}{(1 - \pi_1)}, \ 2 \le k \le N\right\}$$
 (3)

and for  $2 \le I < m \le N$ ,

$$F(\mu_{I}, \mu_{m}) = \pi_{1} f(\mu_{1}) + \frac{f(\mu_{m}) - f(\mu_{I})}{\mu_{m} - \mu_{I}} (\delta - \pi_{1} \mu_{1})$$

$$+ \frac{\mu_{m} f(\mu_{I}) - \mu_{I} f(\mu_{m})}{\mu_{m} - \mu_{I}} (1 - \pi_{1}).$$
(4)

#### **Min Cost: Dynamic Parameters**

#### **Theorem**

If  $k^* = 2$ , the minimal cost is

$$\min_{\pi_2, \dots, \pi_N} \Phi(\pi_2, \dots, \pi_N) = \pi_1 f(\mu_1) + (1 - \pi_1) f(\mu_2),$$

which is reached by launching MTD to induce configuration  $C_2$  only. If  $k^* > 2$ , the minimal cost is

$$\min_{\pi_2, \dots, \pi_N} \Phi(\pi_2, \dots, \pi_N) = \min_{I < k^* \le m} F(\mu_I, \mu_m) = F(\mu_{I^*}, \mu_{m^*}). \tag{5}$$

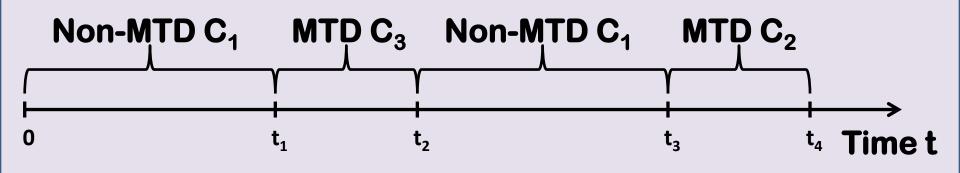
The minimal cost is reached by launching MTD to induce configurations  $C_{l^*}$ ,  $C_{m^*}$  respectively with portions of time:

$$\begin{bmatrix} \pi_{I^*} \\ \pi_{m^*} \end{bmatrix} = \frac{1}{\mu_{m^*} - \mu_{I^*}} \begin{bmatrix} (\mu_{m^*} - \delta) + \pi_1(\mu_1 - \mu_{m^*}) \\ -(\mu_{I^*} - \delta) + \pi_1(\mu_{I^*} - \mu_1) \end{bmatrix}.$$
 (6)

where  $0 < \delta \ll 1$  is some constant.

### Algorithm for Orchestrating MTD to Achieve the Min Cost

- 1. Compute  $k^*$  according to (3)
- 2. If  $k^* = 2$ , wait in  $C_1$  for time  $T_1 \leftarrow \exp(a/\pi_1)$  and launch MTD to stay in  $C_2$  for time  $T_2 \leftarrow \exp(a/\pi_2)$  alternately.
- 3. else compute  $\mu_{I^*}, \mu_{m^*} \& \pi_{I^*}, \pi_{m^*}$  according to (5)-(6). endif
- 4. Wait for time  $T_1 \leftarrow \exp(a/\pi_1)$  {system in  $C_1$ }
- 5. Set  $\Delta = \{I^*, m^*\}, j \leftarrow_R \Delta$ ,
- 6.  $T_i \leftarrow \exp(a/\pi_i)$ .
- 7. Launch MTD to stay in  $C_i$  for  $T_i$ .



#### **Simplifications**

- □ When the cost functions are convex or concave, things can be simplified
  - True for many practical scenarios
- □ See paper for details

#### Roadmap

- □ Cyber epidemics model accommodating MTD
- $\square$  Analysis: The case of dynamic parameters  $\beta(t)$ ,  $\gamma(t)$
- □ Analysis: The case of dynamic structures G(t)
- □ Related work
- Conclusion and future research directions

#### **A General Result**

#### **Theorem**

(a general result) Consider  $C_l = (G_l, \beta, \gamma)$ ,  $l = 1, \dots, N'$ , where  $C_\ell = (G_\ell, \beta, \gamma)$  for  $1 \le \ell \le j$  violate condition (1) but  $C_k = (G_k, \beta, \gamma)$  for  $j < k \le N'$  satisfy condition (1). Then, MTD is effective if G(t) are driven by Markov process strategy  $\sigma_t$  with infinitesimal generator  $Q = (q_{uv})_{N' \times N'}$  defined as:

(i) for 
$$k > j$$
,  $-q_{kk} \le \frac{2a[\beta - \gamma \lambda_1(A_k) - \delta]}{\frac{jc + N' - 1 - j}{N' - 1} - a}$ ;

(ii) for 
$$\ell \leq j$$
,  $-q_{\ell\ell} \geq \frac{2b[\gamma\lambda_1(A_{\ell})-\beta+\delta]}{b-\frac{c(j-1)}{N'-1}-\frac{N'-j}{N'-1}}$ ;

(iii) 
$$q_{rp} = \frac{-q_{rr}}{N'-1}$$
 for all  $p \neq r$  and  $p, r \in \{1, ..., N'\}$ .

here  $0 < \delta \ll 1$ , c is related to the convergent speed, a, b, c are arbitrary constants with a < 1 < b < c.

#### **Max Tolerance of Insecure Configuration** without Considering MTD Cost

#### Theorem

For configurations  $C_j = (G_j, \beta_1, \gamma_1)$  with  $1 \le j \le N'$ , we have  $\mu_j = \beta_1 - \gamma_1 \lambda_1(A_j)$  and  $\mu_1 < 0 < \mu_2 < \cdots < \mu_{N'}$ . The maximal potion of time the system can afford to stay in configuration  $C_1$  is

$$\pi_1^* = \frac{\frac{b-1}{2b[-\mu_1 + \delta]}}{\frac{b-1}{2b[-\mu_1 + \delta]} + \frac{c-a}{2a[\mu_{N'} - \delta]}},$$
(7)

where  $0 < \delta \ll 1$ , a < 1 < The optimalMTD to induce  $C_{N'}$  only w orchestration strategy V

$$\pi_{N'}^* = 1 - \pi_1^*.$$

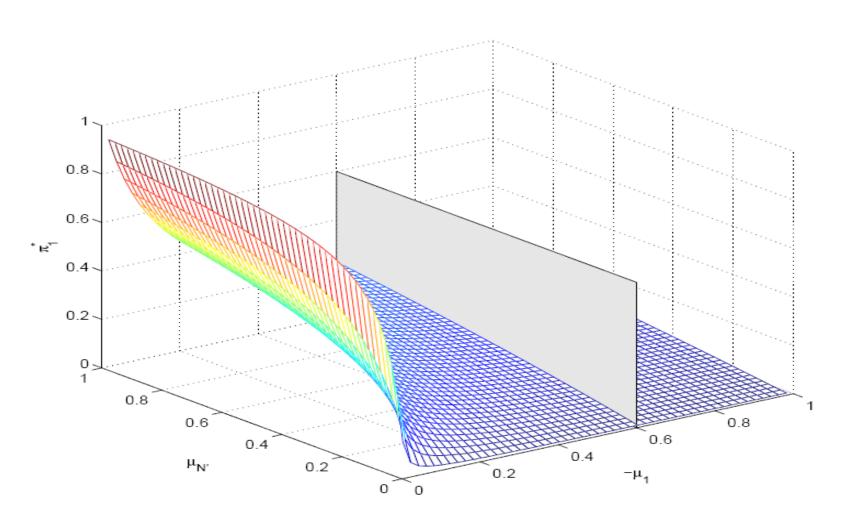
by launching

## Algorithm for Orchestrating MTD to Achieve the Maximum Tolerance (without considering cost)

- 1. Compute  $\pi_1^*$  according to (7).
- while TRUE do
- 3. Wait for time  $T_1 \leftarrow \exp(a/\pi_1^*)$  {system in  $C_1$ }
- 4. Launch MTD to make system stay in  $C_{N'}$  for time  $T_{N'} \leftarrow \exp(a/(1-\pi^*))$

Non-MTD  $C_1$  MTD  $C_N$ , Non-MTD  $C_1$  MTD  $C_N$ ,  $t_1$   $t_2$   $t_3$   $t_4$  Time t

## Degree of Tolerance vs. Parameters: the case of not considering cost



Dependence of  $\pi_1^*$  on  $-\mu_1$  and  $\mu_{N'}$ .

## Minimizing Cost w.r.t. Given Degree of Tolerance

#### Idea for finding min cost:

- 1. Consider possible combinations of MTD-induced configurations:  $\mathcal{L}_1, \dots, \mathcal{L}_{2^{N'-1}}$
- 2. Find  $\sigma_t$  (according to previous theorem) such that MTD forces the convergen Fortunately, the number of MTD-induced configurations of the state of the state
- 3. For each  $\mathcal{L}_i$  with valid denoted by  $\pi_1^i$ , the M TD allows the system to stay in  $\mathcal{C}_1$ . If  $\pi_1^i \geq \pi_1$ , keep  $\mathcal{L}_i$ ; otherwise, eliminate  $\mathcal{L}_i$ .
- 4. For the remaining  $\mathcal{L}_{j}$ 's, compute the minimum cost of launching MTD corresponding to it.
- 5. Find the minimum cost among the costs.

#### **Finding Minimum Cost**

Suppose  $\pi_1$ , where  $\pi_1 \leq \pi_1^*$ , is the potion of time the system must stay in  $C_1$  and  $g(\cdot)$  is the cost function.

 $\sigma_t$  defines the deployment of MTD: denote  $Q = [q_{jk}]$  its infinitesimal generator,  $x_l = \frac{1}{-q_{ll}}$  the expectation of sojourn time in  $C_l$ . Then, the portion of time in  $C_l$  is  $\pi_l = \frac{x_l}{\sum_j x_j}$ .

Suppose MTD induces  $C_{k_1}, \cdots, C_{k_{m'}}$ , the cost of this MTD is

$$\Phi(\pi_2, \dots, \pi_N) = \pi_1 g(\mu_1) + \sum_{j=2}^N \pi_j g(\mu_j)$$

$$= \pi_1 g(\mu_1) + (1 - \pi_1^*) \frac{\sum_{l=1}^{m'} x_{k_l} g(\mu_{k_l})}{\sum_{l=1}^{m'} x_{k_l}}.$$

#### **Finding Minimum Cost**

#### **Theorem**

Find  $\{k_1^*, \cdots, k_m^*\}$  such that

$$\{\mu_{k_1^*}, \cdots, \mu_{k_m^*}\} = \arg\min_{\{k_1, \cdots, k_{m'}\} \in \mathcal{K}} G(k_1, \cdots, k_{m'})$$
 (8)

For given cost function  $g(\cdot)$ , the minimum cost is

$$\Psi(\bar{x}_1,\bar{x}_{k_1^*}(m)+\Delta,\cdots,\bar{x}_{k_m^*}(m))=\pi_1g(\mu_1)+(1-\pi_1)G(k_1^*,\cdots,k_m^*),$$

which is reached by launching MTD to induce configuration  $\{(G_{k_l^*}, \beta, \gamma)\}_{l=1}^m$  via the following deployment strategy:

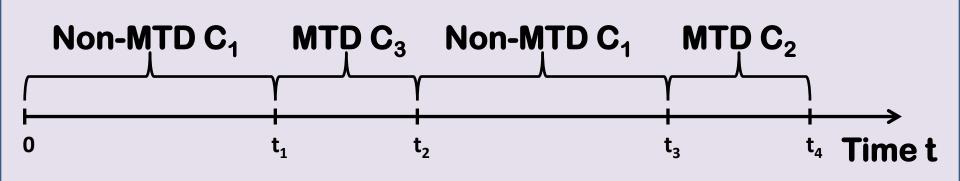
$$\pi_{k_{1}^{*}} = (1 - \pi_{1}) \frac{\bar{x}_{k_{1}^{*}}(m) + \Delta(k_{1}^{*}, \cdots, k_{m}^{*})}{\sum_{l=1}^{m} \bar{x}_{k_{l}^{*}}(m) + \Delta(k_{1}^{*}, \cdots, k_{m}^{*})},$$

$$\pi_{k_{l}^{*}} = (1 - \pi_{1}) \frac{\bar{x}_{k_{l}^{*}}(m)}{\sum_{l=1}^{m} \bar{x}_{k_{l}^{*}}(m) + \Delta(k_{1}^{*}, \cdots, k_{m}^{*})},$$

$$I = 2, \cdots, m.$$
(9)

## Algorithm for Orchestrating MTD to Achieve the Minimum Cost

- 1. Compute  $k_1^*, \dots, k_m^*$  and  $\pi_{k_1^*}, \dots, \pi_{k_1^*}$  according to (8)-(9)
- 2. Wait for time  $T_1 \leftarrow \exp(a/\pi_1)$  {system in  $C_1$ }
- 3. Set  $\Delta = \{k_1^*, \cdots, k_m^*\}, k_i^* \leftarrow_R \Delta$
- 4.  $T_{k_i^*} \leftarrow \exp(a/\pi_{k_i^*})$
- 5. Launch MTD to stay in  $C_{k_i^*}$  for time  $T_{k_i^*}$
- 6. Set  $\Delta = \{1, k_1^*, \dots, k_m^*\} \{k_i^*\}, k_i^* \leftarrow_R \Delta$



#### Roadmap

- □ Cyber epidemics model accommodating MTD
- $\square$  Analysis: The case of dynamic parameters  $\beta(t)$ ,  $\gamma(t)$
- □ Analysis: The case of dynamic structures G(t)
- □ Related work
- Conclusion and future research directions

#### **Related Work**

- ☐ Characterizing effectiveness of MTD: two complementary perspectives (see paper for references):
  - Specific technique with localized view vs.
     classes of techniques with global view
  - ❖ Step closer to real system: state → configuration
- ☐ Cyber Epidemic Dynamics: an active research area rooted in biological epidemic dynamics
  - But beyond it because of unique technical barriers

#### **Limitation of the Study**

- ☐ Assume attack-defense structures and parameters (i.e., transient configurations) are given.
  - Eliminating it: An orthogonal thread of Cybersecurity
     Dynamics (see poster)
- □ Assume attacker cannot choose when to impose configuration C₁.
- **Assume homogeneous parameters**  $\gamma$ (v, u) =  $\gamma$  and  $\beta$ (v) =  $\beta$ .
- Eliminate them or weaken them as much as possible
- Where is the boundary between analytic model and simulation model?

#### **Conclusion and Future Work**

- □ An approach: using cyber epidemic dynamics to characterize the power of MTD.
- □ Two measures of MTD-power: Optimization
- Constructive proofs that lead to algorithms for
  - orchestrating MTD to achieve the maximum
  - tolerance or minimum cost
- ☐ Future work: Addressing the limitations

## Enjoy exploring the unknown territory!





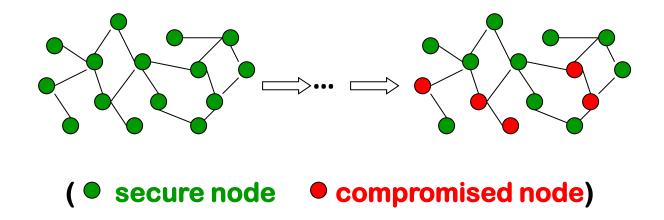












- ☐ Can be instantiated at multiple resolutions: nodes represent (for example) computer, component, etc.
- ☐ Topology can be arbitrary in real-life: from complete graph to any structure

#### The Gap Need to Be Bridged to Practice

We assume we know "transient" capabilities of launching MTD (in terms of manipulating the model parameters).

- ☐ Justification: No single MTD defense (combination) would be "permanently" powerful to force the dynamics converge to desired state (e.g., due to zero-day attacks)
- Many desired "transient" configurations can tolerate some undesired configurations, when making the dynamics converge to the desired equilibrium state

Need to eliminate this assumption.